WKS 2-7 - Chem Honors

Dimensional Analysis 2: Metric Conversions Double Units & Squared/Cubed Units

Use the prefix conversions chart on the reference sheet to convert the measurements in part A. Show all steps needed to convert from starting units to ending units. You must use the proper number of sig figs in your answer.

A. Metric System

1) 40. mL to L

$$\underline{40}$$
. mL $\times \frac{1 \times 10^{-3} \text{ L}}{1 \text{ mL}} = \boxed{0.040 \text{ L}}$

2) 85 g to μg

$$85 \text{ g} \times \frac{1 \text{ µg}}{1 \times 10^{-6} \text{ g}} = \boxed{8.5 \times 10^7 \text{ µg}}$$

3) 6300 m to km

$$\underline{6300} \text{ m} \times \frac{1 \text{ km}}{1 \times 10^3 \text{ m}} = \underline{\underline{6.3} \text{ km}}$$

4) 2.50 kg to g

$$\underbrace{2.50}_{1} \text{ kg} \times \frac{1 \times 10^{3} \text{ g}}{1 \text{ kg}} = \underbrace{2.50 \times 10^{3} \text{ g}}$$

$$544 \text{ ns} \times \frac{1 \times 10^{-9} \text{ s}}{1 \text{ ns}} = \boxed{5.44 \times 10^{-7} \text{ s}}$$

6) 1.92 L to mL

$$?1.92 \cancel{L} \times \frac{1 \text{ mL}}{1 \times 10^{-3} \cancel{L}} = \boxed{1920 \text{ mL} = 1.92 \times 10^{3} \text{ mL}}$$

74.0 cm to km

$$74.0 \text{ cm} \times \frac{1 \times 10^{-2} \text{ m}}{1 \text{ cm}} \times \frac{1 \text{ km}}{1 \times 10^{3} \text{ m}} = \boxed{7.40 \times 10^{-4} \text{ km}}$$

 $4.13 \times 10^{-4} \text{ MW to } \mu\text{W (W = watts)}$

$$\underline{4.13} \times 10^{-4} \text{ MW} \times \frac{1 \times 10^{6} \text{ W}}{1 \text{ MW}} \times \frac{1 \mu \text{W}}{1 \times 10^{-6} \text{ W}} = \underline{\underline{4.13} \times 10^{8} \mu \text{W}}$$

 1.50×10^3 TB to GB (B = bytes)

$$1.50 \times 10^3 \text{ PB} \times \frac{1 \times 10^{12} \text{ B}}{1 \text{ PB}} \times \frac{1 \text{ GB}}{1 \times 10^9 \text{ B}} = \boxed{1.50 \times 10^6 \text{ GB}}$$

B. Double Units & Squared/Cubed Units

Use any needed conversion factors from the previous worksheet.

10) In the US, milk is sold by the gallon, while in Denmark it is sold by the liter. Milk in the US costs \$3.29/gal. What is the equivalent cost in Danish Krone per liter (the exchange rate is 6.3512 DKK/\$1.00 as of Oct. 3, 2020)?

 $\$ \rightarrow DKK$; gal $\rightarrow qts \rightarrow L$

$$\frac{$\frac{3.29}{1 \text{ gal}} \times \frac{1 \text{ gal}}{4 \text{ grs}} \times \frac{1.057 \text{ grs}}{1 \text{ L}} \times \frac{6.3512 \text{ DKK}}{$\frac{1.00}{1 \text{ L}}} = \frac{5.52 \text{ DKK}}{1 \text{ L}} = \frac{5.52 \text{ DKK/L}}{1 \text{ L}}$$

11) The speed of sound in dry air at sea level and 20°C is 343.2 m/s. What would this be in km/day?

$$\frac{343.2 \text{ m}}{1 \text{ s}} \times \frac{1 \text{ km}}{1 \times 10^3 \text{ m}} \times \frac{60 \text{ s}}{1 \text{ min}} \times \frac{60 \text{ min}}{1 \text{ kr}} \times \frac{24 \text{ kr}}{1 \text{ day}} = \frac{29,652}{1 \text{ gay}} = \frac{29,650 \text{ km/day}}{1 \text{ km/day}}$$

12) The energy released when propane (C_3H_8) burns is 2,044 kJ/mol (kilojoules/mole). What is this amount in picojoules/molecule (pJ/mlcl)? (Use the conversion factor 1 mol = 6.022×10^{23} mlcl)

$$kJ \rightarrow J \rightarrow pJ$$
; $mol \rightarrow mlcl$

?
$$\frac{2,044 \text{ kJ}}{1 \text{ mol}} \times \frac{1 \times 10^3 \text{ J}}{1 \text{ kJ}} \times \frac{1 \text{ pJ}}{1 \times 10^{-12} \text{ J}} \times \frac{1 \text{ mol}}{6.022 \times 10^{23} \text{ mlcl}} = \underline{3.394} \times 10^{-6} = \underline{3.394} \times 10^{-6} \text{ pJ/mlcl}$$

13) At an altitude of 10,000 m, the density of air is 4.20×10^{-4} g/cm³. Convert this to μ g/mm³ (remember, to convert a cubed unit, put the *entire* conversion factor into parentheses and cube it).

$$g \rightarrow \mu g; cm^3 \rightarrow m^3 \rightarrow mm^3 (or cm^3 \rightarrow mm^3)$$

$$\frac{4.20 \times 10^{-4} \text{ g}}{\text{cm}^{3}} \times \frac{1 \text{ µg}}{1 \times 10^{-6} \text{ g}} \times \left(\frac{1 \text{ cm}}{1 \times 10^{-2} \text{ m}} \times \frac{1 \times 10^{-3} \text{ m}}{1 \text{ mm}}\right)^{3} = \boxed{0.420 \text{ µg/mm}^{3}}$$

$$\left(\frac{1 \text{ cm}}{10 \text{ mm}}\right)^{3} = \frac{1 \text{ cm}^{3}}{1000 \text{ mm}^{3}}$$

14) In problem #10 you found that milk in Denmark costs 5.52 DKK/L. If the average Danish family uses 208 L of milk each year, how much do they spend, in DKK, on milk in one year?

$$\underline{208} \cancel{L} \times \frac{5.52 \text{ DKK}}{1 \cancel{L}} = \underline{114}8.16 \text{ DKK} = \underline{\boxed{1150 \text{ DKK}}}$$

15) The speed of light in a vacuum is 2.998×10^8 m/s. The average distance from the sun to the earth is 1.496×10^8 km. How much time, in minutes, does light take to travel this distance?

$$km \rightarrow m \rightarrow s \rightarrow min$$

$$\underbrace{\frac{1.496 \times 10^8 \text{ km}}{1 \text{ km}}} \times \underbrace{\frac{1 \times 10^3 \text{ m}}{2.998 \times 10^8 \text{ m}}} \times \underbrace{\frac{1 \text{ min}}{60 \text{ s}}} = \underbrace{8.3167} = \underbrace{8.317 \text{ min}}$$
Relates time to distance

16) Gold has a density of 19.31 g/cm³. An explorer finds a large, pure gold statue and determines its mass to be 11.6 kg. What is the volume, in m³, of this statue? (Remember to cube the conversion factor from cm → m.)

$$kg \rightarrow g \rightarrow cm^3 \rightarrow m^3$$

$$\underbrace{\frac{11.6 \text{ kg} \times \frac{1 \times 10^{3} \text{ g}}{1 \text{ kg}} \times \underbrace{\frac{1 \text{ cm}^{3}}{19.31 \text{ g}}}_{\text{Relates mass to volume}} \times \underbrace{\left(\frac{1 \times 10^{-2} \text{ m}}{1 \text{ cm}}\right)^{3}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ cm}^{3}}{1 \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ cm}^{3}}{1 \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ cm}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}{1 \times 10^{-6} \text{ cm}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ e}}{6.01 \times 10^{-4} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}} = \underbrace{\frac{6.007 \times 10^{-4} \text{ m}^{3}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}}_{\frac{1 \times 10^{-6} \text{ m}^{3}}}_{\frac{1$$

17) The average neon (Ne) atom has a mass of 20.18 amu/atom (atomic mass unit = amu). 1 amu = 1.661×10^{-24} g. If the typical Ne light holds 1.00×10^{15} Ne atoms, what mass of neon, in kg, is in the Ne light?

$$atoms \rightarrow amu \rightarrow g \rightarrow kg$$

$$\underline{1.00} \times 10^{15} \text{ Ne atoms} \times \frac{20.18 \text{ armu}}{1 \text{ Ne atom}} \times \frac{1.661 \times 10^{-24} \text{ g/s}}{1 \text{ armu}} \times \frac{1 \text{ kg}}{1 \times 10^3 \text{ g/s}} = \underline{3.35} \times 10^{-11} = \underline{\boxed{3.35} \times 10^{-11} \text{ kg}}$$