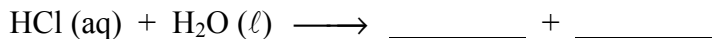


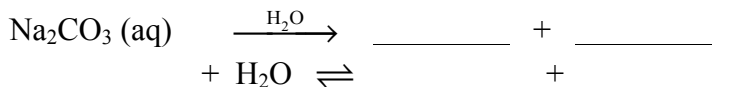
**Part I:  $K_w$  and the relationship between  $H_3O^+$  and  $OH^-$**

**A) An introduction: Rainbow Demonstration**

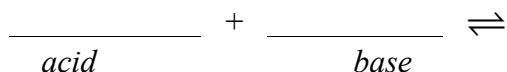
Solution 1: Start with 0.1 M HCl (aq) containing Universal Indicator. It is red. Why? \_\_\_\_\_



Solution 2: Saturated  $Na_2CO_3$  (aq) with universal indicator. It is violet. Why? \_\_\_\_\_



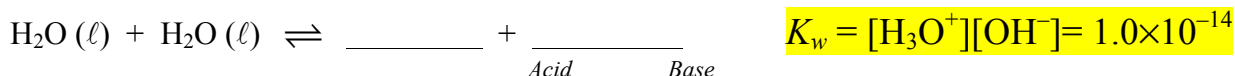
Now, saturated  $Na_2CO_3$  (aq) is added to HCl (aq). An acid-base reaction occurs.



RED ORANGE	Excess $H_3O^+$ ; Solution is Acidic (pH < 7): $[H_3O^+]$ is ( <b>high, low</b> ); $[OH^-]$ is ( <b>high, low</b> )
GREEN	Same moles of $H_3O^+$ and $CO_3^{2-}$ ; Soln is Neutral (pH = 7) $[H_3O^+]$ and $[OH^-]$ are _____
BLUE VIOLET	Excess $CO_3^{2-}$ ; Solution is Basic (pH > 7): $[H_3O^+]$ is ( <b>high, low</b> ); $[OH^-]$ is ( <b>high, low</b> )

Thus, the relationship between  $[H_3O^+]$  and  $[OH^-]$  is (**direct, inverse**).

**B) Concept of Self-Ionization of Water (Concept of  $K_w$ : The equilibrium constant for water)**



Now, use Le Châtelier's Principle:

- If  $[H_3O^+]$ , an acid, is added to water, the equilibrium shifts to the \_\_\_\_\_ which causes the  $[OH^-]$  to \_\_\_\_\_
- If  $[OH^-]$ , a base, is added to water, the equilibrium shifts to the \_\_\_\_\_ which causes the  $[H_3O^+]$  to \_\_\_\_\_

1) **Given either  $[H_3O^+]$  or  $[OH^-]$ , calculate the value asked. Then, determine if the solution is acidic, neutral or basic and circle A, N or B.**

- a)  $[H_3O^+] = 0.1 \text{ M}$   $[OH^-] = ?$  A, N, B ?  
 (Acidic, neutral, basic?)
- d)  $[H_3O^+] = 8.9 \times 10^{-9} \text{ M}$   $[OH^-] = ?$  A, N, B ?
- b)  $[OH^-] = 0.0001 \text{ M}$   $[H_3O^+] = ?$  A, N, B ?
- e)  $0.025 \text{ M KOH}$   $[H_3O^+] = ?$  A, N, B ?
- c)  $0.001 \text{ M HCl}$   $[OH^-] = ?$  A, N, B ?
- f)  $0.0075 \text{ M Ca(OH)}_2$   $[H_3O^+] = ?$  A, N, B ?

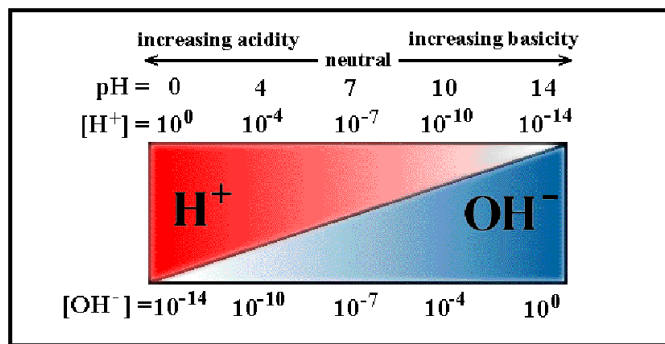
## Part II: pH and pOH

### A) pH: Power of hydronium ion concentration

$$\text{pH} = -\log [\text{H}_3\text{O}^+]; [\text{H}_3\text{O}^+] = 10^{-\text{pH}}$$

- 2) Given the following  $[\text{H}_3\text{O}^+]$  values, determine the pH of each solution. Circle either A, N, B.

Note: Determining sig figs is tricky when dealing with logs. The rule is that the number of sig figs of the  $[\text{H}_3\text{O}^+]$  value is equal to the number of decimal places in the pH value.



a)  $[\text{H}_3\text{O}^+] = 1.0 \times 10^{-3} \text{ M}$

b)  $[\text{H}_3\text{O}^+] = 1.0 \times 10^{-7} \text{ M}$

c)  $[\text{H}_3\text{O}^+] = 1.0 \times 10^{-12} \text{ M}$

pH = \_\_\_\_\_ A, N, B?

pH = \_\_\_\_\_ A, N, B?

pH = \_\_\_\_\_ A, N, B?

d)  $[\text{H}_3\text{O}^+] = 6.5 \times 10^{-11} \text{ M}$

e)  $[\text{H}_3\text{O}^+] = 11.5 \times 10^{-6} \text{ M}$

f) 12 M HBr

pH = \_\_\_\_\_ A, N, B?

pH = \_\_\_\_\_ A, N, B?

pH = \_\_\_\_\_ A, N, B?

- 3) Given the following pH values, determine the  $[\text{H}_3\text{O}^+]$  for the solutions. Circle either A, N, B.

a) pH = 11.00 A, N, B?

b) pH = 3.87 A, N, B?

c) pH = 8.40 A, N, B?

$[\text{H}_3\text{O}^+] =$  \_\_\_\_\_

$[\text{H}_3\text{O}^+] =$  \_\_\_\_\_

$[\text{H}_3\text{O}^+] =$  \_\_\_\_\_

- 4) Solution A has a pH of 2 and solution B has a pH of 5. Which solution has a higher concentration of  $[\text{H}_3\text{O}^+]$ ? \_\_\_\_\_ How much stronger is that solution than the other solution? Explain your reasoning.

### B) Relationships between pH, pOH, $[\text{H}_3\text{O}^+]$ and $[\text{OH}^-]$

Similarly to pH, pOH is the power of hydroxide ion. Thus,  $\text{pOH} = -\log [\text{OH}^-]$  &  $[\text{OH}^-] = 10^{-\text{pOH}}$ .

Similarly,  $\text{p}K_w = -\log K_w$ . We already know that  $K_w = [\text{H}_3\text{O}^+][\text{OH}^-] = 1.0 \times 10^{-14}$ . Thus, if you take the -log of both sides, one gets...

$$-\log K_w = -\log [\text{H}_3\text{O}^+] + (-\log [\text{OH}^-]) = -\log (1.0 \times 10^{-14})$$

$$\text{p}K_w = \text{pH} + \text{pOH} = 14.00$$

Thus, we now have 6 equations we can use to convert between pH, pOH,  $[\text{H}_3\text{O}^+]$  and  $[\text{OH}^-]$ . To review, those equations are as follows:  $K_w = [\text{H}_3\text{O}^+][\text{OH}^-] = 1.0 \times 10^{-14}$   $\text{pH} + \text{pOH} = 14.00$

$$\text{pH} = -\log [\text{H}_3\text{O}^+] \quad [\text{H}_3\text{O}^+] = 10^{-\text{pH}} \quad \text{pOH} = -\log [\text{OH}^-] \quad [\text{OH}^-] = 10^{-\text{pOH}}$$

- 5) Calculate the pH and pOH of the following solutions of strong acids and bases.

a)  $1.0 \times 10^{-4} \text{ M HI}$

b) 0.050 M  $\text{HNO}_3$

c)  $1.0 \times 10^{-3} \text{ M KOH}$

d)  $2.4 \times 10^{-5} \text{ M Mg(OH)}_2$

6) Use what is given to determine any missing values.

a)	$[\text{H}_3\text{O}^+] = 1.0 \times 10^{-9} \text{ M}$	$[\text{OH}^-] =$	pH=	pOH=	A, N, B
b)	$[\text{H}_3\text{O}^+] =$	$[\text{OH}^-] =$	pH=	<b>pOH= 2.0</b>	A, N, B
c)	$[\text{H}_3\text{O}^+] =$	<b><math>[\text{OH}^-] = 4.5 \times 10^{-8} \text{ M}</math></b>	pH=	pOH=	A, N, B
d)	$[\text{H}_3\text{O}^+] =$	$[\text{OH}^-] =$	<b>pH= 10.76</b>	pOH=	A, N, B

Answers: 1a)  $1 \times 10^{-13} \text{ M}$ ; 1b)  $1 \times 10^{-10} \text{ M}$ ; 1c)  $1 \times 10^{-11} \text{ M}$ ; 1d)  $1.1 \times 10^{-6} \text{ M}$ ; 1e)  $4.0 \times 10^{-13} \text{ M}$ ; 1f)  $6.7 \times 10^{-13} \text{ M}$ ; 2a) 3.00; 2b) 7.00; 2c) 12.00; 2d) 10.19; 2e) 4.939; 2f) -1.08; 3a)  $1.0 \times 10^{-11}$ ; 3b)  $1.3 \times 10^{-4} \text{ M}$ ; 3c)  $4.0 \times 10^{-9} \text{ M}$ ; 5a) pH = 4.00, pOH = 10.00; 5b) pH = 1.30, pOH = 12.70; 5c) pOH = 3.00, pH = 11.00; 5d) pOH = 4.32, pH = 9.68; 6a)  $1.0 \times 10^{-5} \text{ M}$ , 9, 5; 6b)  $1.0 \times 10^{-12} \text{ M}$ ,  $1.0 \times 10^{-2} \text{ M}$ , 12; 6c)  $2.2 \times 10^{-7} \text{ M}$ , 6.65, 7.35; 6d)  $1.7 \times 10^{-11} \text{ M}$ ; 5.8  $\times 10^{-4} \text{ M}$ , 3.24